Contributing Factors to a Country's Happiness

"Happiness" can be quite a subjective term. Some people may be happy if they earn enough to buy them lunch and dinner for their family on a daily basis, while others in the exact same scenario may be grossly unhappy because they believe they deserve more but are being impeded by the current socio-economic situations in their homeland. Even two neighbors who share just a wall between them can have exceedingly mismatched views on their nation's current affairs! We attempted to answer the following questions about the data collected by the World Happiness Report.

- 1. Does a country's income level affect the average level of positive or negative feelings?
- 2. Which features have the greatest impact on a country's happiness and how well can we use these features to predict a country's happiness?
- 3. Can we make predictions about future happiness levels based on the happiness levels over time?
- 4. Do countries with lower levels of happiness have more variability in their happiness levels?

CLASSIFICATION: LOGISTIC REGRESSION

One of the major topics we wanted to explore was whether or not income level affects one's positive or negative feelings. These feelings are captured in the positive and negative affect variables within the dataset. Positive affect was measured as the national average of the binary responses to questions that aim to capture whether the respondent smiled, laughed, or enjoyed during the previous day. Negative affect was measured as the national average of the binary responses to questions that aim to capture whether the respondent smiled, laughed, or enjoyed during the previous day. Negative affect was measured as the national average of the binary responses to questions that aim to capture whether the respondent felt worried, sad, or angry during the previous day. We found this to be an interesting dynamic to explore when visualizing the data, since the graph of negative affect versus positive affect, with high income countries' data points in green and low income countries' data points in red, does not seem to show that the income level majorly affects the way people feel. This graph is shown below.



We decided to use logistic regression to determine how effective the positive and negative affect variables are at predicting a country's income level (High or Low). The binary outcome that the model predicts is income level (0 for low income and 1 for high income). Originally, we fit a straightforward logistic regression model on the full dataset with positive and negative affect as the independent variables. The results showed that positive and negative affect have a significant p-value, at the $\alpha = 0.05$ level, indicating that the model classifies the data well based on positive and negative affect. The positive value of the positive affect's coefficient shows it is positively related with higher income group, and the negative value of the negative affect variable's coefficient indicates it is negatively related with higher income group and positively related with lower income group.

	Lo	git Regr	ression	Result	S		
Dep. Variable	Incon	neGroup	b	No. Ob	servat	ions:	1888
Model:	Logit			Df R	esidua	ls:	1885
Method:	MLE			Df	Model	:	2
Date:	Wed,	19 May	2021	Pseu	do R-s	qu.:	0.03757
Time:	20:01	:12		Log-L	.ikeliho	od:	-1219.2
converged:	True			L	L-Null:		-1266.8
Covariance Typ	e: nonro	bust		LLR	p-valu	le:	2.142e-21
	coef	std err	z	P> z	[0.025	0.975	5]
const	-1.9943	0.434	-4.590	0.000	-2.846	-1.14	3
Positive affect	3.9164	0.490	7.989	0.000	2.956	4.877	,
Negative affect	-1.2553	0.614	-2.044	0.041	-2.459	-0.05	1

To further explore the effect that these variables have, we split the data into a training and test set, using 1/5 of the data for the test set, and chose the best variables by minimizing the Aikake Information Criterion (AIC) of the model. The variables selected to obtain the minimum AIC were both the positive affect and negative affect variable, which supports our previous results. When using this model to make predictions on the test set, it achieved an accuracy of 0.6269841. This is pretty good considering there are only two predictors and the test accuracy is clearly better than random.

	Logit Regression Results						
Dep. Variable:	Incon	neGroup	o No	o. Obs	ervatio	ns:	1888
Model:	Logit			Df Res	siduals	:	1885
Method:	MLE			Df N	lodel:		2
Date:	Fri, 2	1 May 2	021	seudo	R-squ	ı.:	0.03757
Time:	02:08	:24	L	.og-Lik	elihoo	d:	-1219.2
converged:	True			LL-	Null:		-1266.8
Covariance Type	e: nonro	bust		LLR p	-value		2.142e-21
	coef	std err	z	P> z	[0.025	0.9	75]
const -	1.9943	0.434	-4.590	0.000	-2.846	-1.1	143
Positive affect	3.9164	0.490	7.989	0.000	2.956	4.8	77
Negative affect -	1.2553	0.614	-2.044	0.041	-2.459	-0.0	051

In order to extend the analysis and see how the other variables affect the ability to predict income groups using logistic regression, we wanted to do a regression with the whole dataset. We excluded the variable of Log GDP per capita as that is too closely related to income groups. After splitting the data into train and test sets (80/20 split) and selecting the model that minimized AIC cost on the training data, we found that the best variables to use are year, life ladder, social support, healthy life expectancy at birth, negative affect, access to electricity, agricultural land, mortality rate under 5, forest area, military expenditure, and rural population. When we used the model to make predictions on the test set we achieved an accuracy of 0.9081272. This is a high test accuracy rate, which makes sense since we added more predictors.

	Logit Regression							
Dep. Variable:	IncomeGroup	No. Obse	rvations:	1130				
Model:	Logit	Df Resi	iduals:	1119				
Method:	MLE	Df Mo	odel:	10				
Date:	Fri, 21 May 2021	Pseudo	R-squ.:	0.6957				
Time:	02:13:13	Log-Like	elihood:	-230.90				
converged:	True	LL-N	lull:	-758.85				
Covariance Type:	nonrobust	LLR p-	value:	1.686e-	220			
			coef	std err	z	P> z	[0.025	0.975]
	const		206.7859	73.757	2.804	0.005	62.226	351.346
	year		-0.0956	0.037	-2.614	0.009	-0.167	-0.024
L	ife Ladder		0.6252	0.215	2.914	0.004	0.205	1.046
Healthy life	expectancy at b	irth	-0.1895	0.058	-3.278	0.001	-0.303	-0.076
Ne	gative affect		-5.5734	1.737	-3.208	0.001	-8.978	-2.169
Access to elec	tricity (% of popu	ulation)	0.0415	0.015	2.714	0.007	0.012	0.071
Agricultural	land (% of land a	irea)	-0.0446	0.009	-4.861	0.000	-0.063	-0.027
Mortality rate, un	der-5 (per 1,000 li	ve births)	-0.0848	0.017	-4.910	0.000	-0.119	-0.051
Forest ar	ea (% of land are	a)	0.0219	0.009	2.537	0.011	0.005	0.039
Military exp	enditure (% of G	DP)	0.2507	0.122	2.055	0.040	0.012	0.490
Rural population	n (% of total pop	ulation)	-0.0998	0.011	-9.112	0.000	-0.121	-0.078

These findings suggest that, contrary to what we originally expected, a country's positive affect and negative affect in life is indicative of their income level when observed independently of other variables. In this case a greater positive affect corresponds with a higher income group, and a greater negative affect corresponds to a lower income group. However, when considered with all the variables from the dataset, positive affect is no longer selected when minimizing AIC, while negative affect is selected as a good predictor to use. This suggests that overall, a country's negative affect rate appears to be a more important factor in predicting the country's income level in the context of the rest of the data provided.

LINEAR REGRESSION

Many factors contribute to a country's level of happiness. Given the data provided, we want to determine which factors can be used to best predict a country's level of happiness at a given point in time, perhaps also suggesting which factors a country could focus on improving to make their country happier. To accomplish this, we can use linear regression to fit the data to a model that best represents each factor's relation to a country's happiness level.

Feature Selection

The first step is to select the features that are the best predictors of happiness. Since the data has many (more than 20) features, making a linear regression model using all features will likely result in overfitting. To alleviate this risk, we adopt a "bottom-up" strategy, starting with a single best feature and building up to the 10 best features for predicting the happiness score.

To start this process, we split the data into a training and testing set, with one-third of the records in the testing set. Then we construct a linear regression model using the training data with one feature at a time. In order to select the best features, we select the feature that results in the highest R-squared value, accounting for the largest amount of variance, from its respective model. Next, we then pair this variable with all other variables one at a time and find the model with the best R-squared value. This would mean that those two features paired together make the best model. Similarly, we iterate through, until we have our set of top-10 variables that best predict happiness.

In order to use linear regression, we must test that our data meets the assumptions made by linear regression models.

Testing assumptions

Assumption 1: Check mutual independence of residuals:

To test that the residuals are mutually independent, we can plot the autocorrelation function. In the plot, we observed that none of the autocorrelations are outside the test bounds, indicating that the residuals are independent of each other.

Assumption 2: Check whether the residuals are independent of the covariates:

To test whether the residuals are independent of the covariates, we plot the residuals versus the covariates and analyze the average of the residuals using the "window trick".



From the below plots of residuals vs each covariate, we

do not see any discernible pattern. On the plots, the black lines are the mean value of the residuals in each "window", and we have set the number of windows as 5. The mean value in each plot seems to be centered around the zero mark and the mean also does not change much as the covariates change.



Assumption 3: Check whether the residuals are normally distributed:

To test whether the residuals are normally distributed, we can use a kernel density estimate (KDE) plot and a QQ-plot.



The QQ-plot seems like a convex-concave type, having light tails. A normal distribution has values of skewness and kurtosis as zero, and as we see from the KDE plot, the skewness and kurtosis of the distribution are well within the acceptable range to be classified as fairly normal, if not exactly so.

Assumption 4: Check whether the residuals have a constant variance:

To test that the residuals have constant variance, we plot the absolute value of the residuals against the fitted values of the covariants. We use the "window trick" to determine if the average of the absolute value of residuals remains relatively constant.



From the above charts, we see that the absolute values of the residuals are independent of the covariates, indicating a fairly homoscedastic nature.

Since all four linear regression assumptions have been met, we can use linear regression with the selected features to make predictions about a country's level of happiness.

Model

After determining that the data meets the assumptions and finding which features to use, we train the model on the training data and obtain the following results:											
0	LS Regression Results					coef	std err	t	P> t	[0.025	0.975]
	Dep. Variable:	Life Ladder	R-squared:	0.792	const	5.3769	0.020	266.531	0.000	5.337	5.417
	Model:	OLS	Adj. R-squared:	0.790	Log GDP per capita	0.5030	0.049	10.217	0.000	0.406	0.600
	Markhard.	1 0	E . 4. 41. 41	250.0	Positive affect	0.1364	0.025	5.429	0.000	0.087	0.186

Method:Least SquaresF-statistic:336.0Generositi0.1360.016.0880.000.0950.116Date:Thu, 20 May 2021Prob (F-statistic):1.30e-310Rural population (% of total population)0.0740.0340.210.0300.1410.007Time:23:50:13Log-Likelihooci-713.45Methodi:Methodi:0.0360.0260.0380.0000.1610.202No. Observations:9046AAIC:1449.Metalthylife expectancy at birl0.3690.0477.8050.0000.2760.406Df Residuals:9035BBC:1502.1502.Metalthylife expectancy at birl0.3640.0477.8050.0000.2760.406Df Model:10Covariance Type:nonrobust101010101010101010101010101010101010Di Adatistic:10Di Adatistic:10Di Adatistic:10Di Adatistic:10101010101010101010101010101	Positive affect 0.1364 0.025 5.429 0.000				
Date: Thu, 20 May 2021 Prob (F-statistic): 1.30e-310 Rural population (% of total population) 0.001 0.003 0.21.70 0.003 0.010 0.003 0.010 0.003 0.010 0.003 0.010 0.003 0.010 0.003 0.010 0.003 0.010 0.003 0.010 0.003 0.010 0.003 0.003 0.010 0.003<	Generosity 0.1356 0.021 6.588 0.000	356.0	F-statistic:	Least Squares	Method:
Time: 23:50:13 Log-Likelihood: -713.45 No. Observations: 946 Alc: 1449. Df Residuals: 935 BIC: 1502. Model: 100 1502. 1502. Df Model: 100 0.000 <th>Rural population (% of total population) -0.0743 0.034 -2.179 0.030 -</th> <th>1.30e-310</th> <th>Prob (F-statistic):</th> <th>Thu, 20 May 2021</th> <th>Date:</th>	Rural population (% of total population) -0.0743 0.034 -2.179 0.030 -	1.30e-310	Prob (F-statistic):	Thu, 20 May 2021	Date:
No. Observations: 946 AIC: 1449. Healthy life expectancy at birth 0.438 0.052 8.43 0.00 0.338 0.464 Df Residuals: 935 BIC: 1502. Motality rate, under-5 (per 1,000 live births) 0.364 0.067 7.805 0.000 0.276 0.462 Df Model: 10 Perceptions of corruption 0.1027 0.000 0.508 0.000 0.263 0.516 Covariance Type: nonrobust nonrobust state state state state state state	Social support 0.2316 0.026 9.036 0.000	-713.45	Log-Likelihood:	23:50:13	Time:
Df Residuals: 935 BIC: 1502. Mortality rate, under-5 (per 1,000 live births) 0.364 0.047 7.805 0.000 0.276 0.462 Df Model: 10 10 Perceptions of corruption -0.017 0.020 -5.093 0.000 -0.142 -0.003 Covariance Type: nonrobust the state of the s	Healthy life expectancy at birth 0.4382 0.052 8.431 0.000	1449.	AIC:	946	No. Observations:
x0_North America 0.3841 0.067 5.756 0.000 0.253 0.515 Df Model: 10 Perceptions of corruption -0.1027 0.020 -5.093 0.000 -0.142 -0.063 Covariance Type: nonrobust x0_South America 0.3164 0.808 3.969 0.000 10.47	ortality rate, under-5 (per 1,000 live births) 0.3694 0.047 7.805 0.000	1502.	BIC:	935	Df Residuals:
Covariance Type: nonrobust nonrobust x0_south America 0.3164 0.080 3.969 0.000 -0.102 -0.000	x0_North America 0.3841 0.067 5.756 0.000			10	Df Model:
Covariance Type: nonrobust x0_South America 0.3164 0.080 3.969 0.000 0.160 0.473	Perceptions of corruption -0.1027 0.020 -5.093 0.000 -			10	Di moden
	x0_South America 0.3164 0.080 3.969 0.000			nonrobust	Covariance Type:

In the model, the R-squared value is 0.792, meaning that 79.2% of the variability in life ladder (happiness level) is accounted for by the features in the model. Additionally, all of the features have p-values of less than 0.05, indicating these features are useful additions to the model in predicting happiness level.

After making the predictions on the test data, we calculate the root mean square error (RMSE) to determine how accurately the model predicts happiness on this data. The RMSE for our model is 0.5, indicating that our predictions on the testing data are on average within 0.5 of the actual value.



TIME-SERIES FORECASTING

Each year, the level of happiness of individual countries as well as the average happiness level of the world changes. Some countries, such as Denmark, have a remarkably high mean happiness level, while others, such as Zimbabwe, have relatively low average happiness levels.

We decided to analyze the average happiness of each of the top 4 happiest countries, bottom 4 happiest countries, and the world to make predictions and forecast the happiness levels of these countries and the world for the next two years. We first constructed linear regression models for each country as well as the world. Below we plotted the actual measurements and the linear regression model's predictions of happiness levels for the years 2015 through 2020.

Country	R ²	Adj R ²	F Statistics	Prob	AIC
		_			
Zimbabwe	0.570	0.463	5.312	0.0825	4.311
Tanzania	0.245	0.056	1.299	0.318	4.457
Jordan	0.978	0.973	181.5	0.000176	-11.50
India	0.233	0.041	1.215	0.332	7.318
Switzerland	0.068	-0.165	0.2914	0.618	-9.806
Denmark	0.115	-0.106	0.5205	0.511	-12.25
Iceland	0.627	0.503	5.041	0.110	-20.61
Finland	0.754	0.692	12.26	0.0249	-10.29
World Average	0.777	0.721	13.90	0.0203	-10.74



The adjusted R-squared values found for each of the countries as well as the world average suggest that the linear regression model does a poor job of fitting the data for most of these countries. To make better predictions and extrapolate predictions into the future, we can use simple exponential smoothing or Holt's method. Since the plots do not show any particular seasonality in the data, we decided not to use Holt-Winters forecasting.

Country	Simple Exponential Smoothing			Holt's Method			
	2021	2022	SSE	2021	2022	SSE	
Zimbabwe	3.13	3.13	0.91	2.86	2.67	0.95	
Tanzania	3.46	3.46	0.50	3.99	4.18	1.14	
Jordan	4.09	4.09	0.42	3.84	3.57	0.19	
India	3.98	3.98	0.80	3.98	3.94	1.20	
Switzerland	7.54	7.54	0.04	7.58	7.59	0.10	
Denmark	7.59	7.59	0.03	7.65	7.66	0.04	
Iceland	7.57	7.57	0.01	7.57	7.58	0.00	
Finland	7.89	7.89	0.08	7.98	8.07	0.05	
World Average	5.83	5.83	0.08	6.09	6.36	0.05	



Simple Exponential Smoothing



 Simple exponential smoothing forecasts the data without taking into account the trend of the data over time. Therefore, the resulting forecasted happiness level remains constant over 2021 and 2022. The chart above outlines both the forecasted happiness level as well as the sum of squared errors (SSE) for each country. Similarly to simple exponential smoothing, Holt's method also forecasts the data. However, it also takes into account the trend of the happiness levels over time when making predictions. For example, countries with happiness levels that appear to trend downward will have a continued downward trend in the forecasted happiness. The above chart also outlines the forecasted happiness levels and SSEs for each country using Holt's method.

One particularly interesting trend in the SSEs that we noticed is that the countries with lower happiness scores had higher SSEs for both forecasting models. This seems to suggest some instability in the happiness scores of these countries over time which can be observed in the differences between actual and fitted values. This also supports the plot from Milestone 1 indicating that countries with higher average happiness scores had a lower standard deviation of happiness scores shown below. We think this could be due to the fact that this variation could reflect instability within the country.



Additionally, with the exception of Tanzania, countries with lower happiness scores seemed to have a decreasing trend in happiness whereas countries with higher scores have an increasing trend in happiness as indicated by the increasing and decreasing forecasts made by Holt's method.

When choosing which forecasting method to use, we compared the SSEs of the countries between the two models. It is not clear which model is better overall for forecasting because Simple Exponential Smoothing has a lower SSE for some countries while Holt's Method has a lower SSE for others. When looking at the world average happiness scores, Holt's Method has a slightly lower SSE. When Holt's method performs better, this suggests that a country's happiness level over time follows a clearer trend either upward or downward.

CONCLUSION

After conducting these different analytical methods, we were able to answer our proposed questions and extend our analysis. We quantified a relationship between positive and negative affect and income level, identified the variables that affect overall happiness the most while creating a linear model, and forecasted happiness levels for a few countries for the next two years while exploring the relationship between the variability of happiness and the average happiness.

Appendix

Logistic Regression:

```
#math
import numpy as np
import random
#dataframes
import pandas as pd
#plotting
import matplotlib.pyplot as plt
#regression tools
import statsmodels.api as sm
from patsy import dmatrices
from sklearn.model selection import train test split
from sklearn.feature selection import SelectFromModel
from sklearn.linear model import LassoCV
#visualization tools
import seaborn as sns
df=pd.read csv('final dataset.csv')
#drop rows with null values
imp=df[['Positive affect', 'Negative affect', 'IncomeGroup']]
imp=imp.dropna()
#replace lower middle income and lower income with 0; and upper middle and
upper with 1
imp['IncomeGroup'] = imp['IncomeGroup'].replace(['Lower middle income','Low
income'], 0)
imp['IncomeGroup']=imp['IncomeGroup'].replace(['Upper middle income', 'High
income'], 1)
#fit logistic regression on full data set for preliminary observations
X = sm.add constant(imp.drop(['IncomeGroup'],axis=1))
y = imp['IncomeGroup']
model = sm.Logit(y,X).fit()
model.summary()
#split train and test
X train, X test, y train, y test = train test split(X, y, test size=0.2,
random state=0)
#cost function
def minAIC(X,y):
    variables = X.columns
```

```
model = sm.Logit(y,X[variables]).fit()
    while True:
        maxp = np.max(model.pvalues)
        newvariables = variables[model.pvalues < maxp]</pre>
        newmodel = sm.Logit(y,X[newvariables]).fit()
        if newmodel.aic < model.aic:
            model = newmodel
            variables = newvariables
        else:
            break
    return model, variables
# select on training set, fit on test set
model,variables = minAIC(X train, y train)
model = sm.Logit(y train, X train[variables]).fit()
model.summary()
res=(model.predict(X test[variables])>=0.5).astype(int)
error=((abs(res-y test)).sum())/len(y test)
#test accuracy
accuracy=1-error
#get full data set for regression
#drop rows with null values
imp2=df.drop(['Region','Continent','Country name','Log GDP per
capita'],axis=1)
imp2=imp2.dropna()
#replace lower middle income and lower income with 0; and upper middle and
upper with 1
imp2['IncomeGroup'] = imp2['IncomeGroup'].replace(['Lower middle
income', 'Low income'], 0)
imp2['IncomeGroup']=imp2['IncomeGroup'].replace(['Upper middle
income', 'High income'], 1)
#fit logistic regression
X = sm.add constant(imp2.drop(['IncomeGroup'],axis=1))
y = imp2['IncomeGroup']
#split train and test
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2,
random state=0)
# select on training set, fit on test set
model,variables = minAIC(X train, y train)
model = sm.Logit(y_train,X_train[variables]).fit()
model.summary()
```

```
res=(model.predict(X_test[variables])>=0.5).astype(int)
error=((abs(res-y_test)).sum())/len(y_test)
#test accuracy
accuracy= 1-error
```

Linear Regression:

```
import pandas as pd
import numpy as np
import statsmodels.api as sm
import matplotlib.pyplot as plt
%matplotlib inline
import seaborn as sns
from sklearn.model selection import train test split
from sklearn.preprocessing import OneHotEncoder, StandardScaler
from sklearn.compose import ColumnTransformer
from sklearn.metrics import mean squared error
plt.rcParams.update({'font.size': 14, 'xtick.labelsize': 15,
'ytick.labelsize': 15})
df = pd.read excel('final data/final dataset.xlsx')
df = df.sort values(by='year')
df.head()
df.dropna(inplace=True)
X = df.iloc[:, 3:] # all features
y = df.iloc[:, 2] # the life ladder (happiness score)
# list of all numerical columns
a = X.dtypes
num cols = a[a!= '0'].index.tolist()
X train, X test, y train, y test = train test split(X, y,
test size=0.33, random state=0)
ct = ColumnTransformer([
    ('num', StandardScaler(), num cols),
    ('cat', OneHotEncoder(sparse=False, drop='first'), ['Continent',
'IncomeGroup'])
], remainder='drop')
ft = ct.fit transform(X train)
```

```
ls = ct.transformers [0][2] +
ct.transformers_[1][1].get_feature_names().tolist()
X train = pd.DataFrame(ft, columns=ls)
X train.head()
# resetting the index, since the splitting have made the indexing
# non-continuous, and it trips up statsmodels
X train.reset index(drop=True, inplace=True)
y train.reset index(drop=True, inplace=True)
# finding the top 10 columns:
cols list = list(X train.columns)
high rsq cols = []
for i in range(10):
    max rsq = 0 # initializing with zero as the max rsquared
    max rsq col = None
    for col in cols list:
        model = sm.OLS(y train, sm.add constant(X train[high rsq cols
+ [col]])).fit()
        if model.rsquared > max rsq:
            max rsq = model.rsquared
            max rsq col = col
    print(max rsq col)
    cols list.remove(max rsq col)
    high rsq cols.append(max rsq col)
X_train_hrc = X_train[high_rsq_cols] # hrc: high rsquared columns
model = sm.OLS(y train, sm.add constant(X train hrc)).fit()
model.summary()
TESTING MODEL ASSUMPTIONS:
(ASSUMPTION 1)
plt.acorr(model.resid)
plt.xlabel("Lag", fontsize=15)
plt.ylabel("ACF", fontsize=15)
plt.show()
# plt.savefig('assumption1.jpeg')
```

```
(ASSUMPTION 2)
X = X train hrc.copy()
model = sm.OLS(y train, sm.add constant(X)).fit()
resid = model.resid
fiq, axes = plt.subplots(2,5, figsize=(30,10), sharey=True)
r, c = 0, 0
windows = 5 # user-specified number of windows.
for col in X.columns: # X is the dataframe of all the covariates
    if col == 'Healthy life expectancy at birth':
        r, c = 1, 0
    axes[r][c].scatter(X[col], resid)
    axes[r][c].set title(col)
    axes[r][c].set ylabel('residual', fontsize=22)
    mn = X[col].min()
    mx = X[col].max()
    bd = np.linspace(mn,mx,windows+1) # the boundaries of each window
    for i in range(windows):
        ixs = []
        low = bd[i]
        high = bd[i+1]
        for ix, vl in enumerate(X[col]):
            if (vl >= low) and (vl <= high): #edited this to make it
closed ended comparison
                ixs.append(ix)
        avg = np.average(resid[ixs])
        divs = 1/(windows)
        axes[r][c].axhline(y=avg, xmin=(i*divs), xmax=(i+1)*divs,
color='k', ls='-.')
    c += 1
plt.show()
# plt.savefig('assumption2.jpeg')
(ASSUMPTION 3)
PART A:
sns.kdeplot(model.resid)
plt.text(y=0.7, x=0.8, s=f'Skew:
{np.round(model.resid.skew(),2)}\nKurtosis:
{np.round(model.resid.kurt(),2)}')
plt.show()
# plt.savefig('assumption3 1.jpeg')
```

```
PART B:
sm.qqplot(model.resid, line='45')
plt.show()
# plt.savefig('assumption3 2.jpeg', pad inches=0)
(ASSUMPTION 4)
X = X train hrc.copy()
model = sm.OLS(y train, sm.add constant(X)).fit()
resid = np.abs(model.resid)
fig, axes = plt.subplots(2,5, figsize=(30,10), sharey=True)
r, c = 0, 0
windows = 5 # user-specified number of windows.
for col in X.columns: # X is the dataframe of all the covariates
    if col == 'Healthy life expectancy at birth':
        r, c = 1, 0
#
     print(r,c)
   axes[r][c].scatter(X[col], resid)
   axes[r][c].set title(col)
   axes[r][c].set_ylabel('| residual |', fontsize=22)
   mn = X[col].min()
   mx = X[col].max()
   bd = np.linspace(mn,mx,windows+1) # the boundaries of each window
   for i in range(windows):
        ixs = []
        low = bd[i]
        high = bd[i+1]
        for ix, vl in enumerate(X[col]):
            if (vl >= low) and (vl <= high): #edited this to make it
closed ended comparison
                ixs.append(ix)
        avg = np.average(resid[ixs])
        divs = 1/(windows)
        axes[r][c].axhline(y=avg, xmin=(i*divs), xmax=(i+1)*divs,
color='k', ls='-.')
   c += 1
plt.show()
# plt.savefig('assumption4.jpeg')
```

```
MODEL TESTING (PREDICTIONS):
```

```
X_test = ct.transform(X_test)
X_test = pd.DataFrame(X_test, columns=1s)
# keeping only the 10 features previously selected, in the test set
X_test_hrc = X_test[high_rsq_cols]
X_test_hrc = sm.add_constant(X_test_hrc)
preds = model.predict(X_test_hrc) # making the predictions
y_test = y_test.reset_index(drop=True)
rmse = np.sqrt(mean_squared_error(y_test, preds))
print(rmse)
plt.scatter(y_test, preds)
plt.xlabel('Actual scores')
plt.ylabel('Predicted scores')
plt.title("Predicted vs Actual scores")
plt.show()
# plt.savefig("pva.jpeg")
```

Forecasting:

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import statsmodels.api as sm
from datetime import datetime
from statsmodels.tsa.holtwinters import Holt, ExponentialSmoothing,
SimpleExpSmoothing
df = pd.read_csv('final_dataset.csv')
df = df[df['year'] >= 2015]
df2 = df[df['year'] == 2020]
df2 = df[df['year'] == 2020]
df3 = df2.sort_values('Life Ladder')
df3 = df2.head(4)
df4 = df2.tail(4)
df2 = pd.concat([df3, df4], axis = 0)
```

```
countries = df2['Country name']
fig, axs = plt.subplots(3, 3, figsize=(15, 12))
plt.rcParams.update({'font.size': 15, 'xtick.labelsize': 10,
'vtick.labelsize': 10})
indX = 0
indY = 0
rsqr adj = []
for countr in countries:
  dfCountry = df[df['Country name'] == countr]
  X = dfCountry['year']
  y = dfCountry['Life Ladder']
  axs[indX, indY].plot(X, y, color='blue', label='Actual')
  axs[indX, indY].set title(countr)
  axs[indX, indY].set ylim(0, 8)
  X = sm.add constant(X)
  model = sm.OLS(y, X).fit()
  Yhat = model.predict(X)
  print(countr)
  print(model.summary())
  rsqr adj.append(model.rsquared)
  axs[indX, indY].plot(X['year'], Yhat, color='red', label='Linear
prediction')
  indX += 1
  if indX > 2:
    indX = 0
    indY += 1
X = df.groupby('year')['Life Ladder'].mean()
X.reset index()
y = X
X = X.index
axs[2, 2].plot(X, y, color='blue', label='Actual')
axs[2, 2].set title('Average overall')
axs[2, 2].set ylim(0, 8)
X = sm.add constant(X)
model = sm.OLS(y, X).fit()
print('World average')
print(model.summary())
rsqr adj.append(model.rsquared adj)
Yhat = model.predict(X)
```

```
axs[2, 2].plot(X[:, 1], Yhat, color='red', label='Linear prediction')
handles, labels = axs[2, 2].get legend handles labels()
fig.legend(handles, labels, loc='upper right')
print(rsqr adj)
fig, axs = plt.subplots(3, 3, figsize=(15, 12))
plt.rcParams.update({'font.size': 15, 'xtick.labelsize': 10,
'ytick.labelsize': 10})
indX = 0
indY = 0
sse = []
for countr in countries:
  dfCountry = df[df['Country name'] == countr]
  X = dfCountry.set index('year')['Life Ladder']
  meanX = X.mean()
  X = X.reindex(range(2015, 2021), fill value=meanX)
  X = X.reindex(range(2015, 2021), fill value=meanX)
  X.index = pd.to datetime(X.index, format='%Y')
  fit = SimpleExpSmoothing(X).fit()
  Yhat = fit.fittedvalues
  fore = fit.forecast(2)
  sse.append(fit.sse)
  fore.index = fore.index.year
  print(countr)
  print(fore)
  print(fit.sse)
  axs[indX, indY].plot(X.index.year, X, color='blue', label='Actual')
  axs[indX, indY].set title(countr)
  axs[indX, indY].set_ylim(0, 9)
  axs[indX, indY].set xlim(2015, 2022)
  axs[indX, indY].plot(Yhat.index.year, Yhat, color='red', label='Fitted
values')
  axs[indX, indY].plot(fore, color='black', label='Forecast')
  indX += 1
  if indX > 2:
    indX = 0
    indY += 1
X = df.groupby('year')['Life Ladder'].mean()
meanX = X.mean()
X = X.reindex(range(2015, 2021), fill value=meanX)
```

```
X.index = pd.to datetime(X.index, format='%Y')
axs[2, 2].plot(X.index.year, X, color='blue', label='Actual')
axs[2, 2].set title('Average overall')
axs[2, 2].set ylim(0, 9)
axs[2, 2].set xlim(2015, 2022)
fit = SimpleExpSmoothing(X).fit()
sse.append(fit.sse)
Yhat = fit.fittedvalues
fore = fit.forecast(2)
fore.index = fore.index.year
print('World average')
print(fore)
print(fit.sse)
axs[2, 2].plot(Yhat.index.year, Yhat, color='red', label='Fitted values')
axs[indX, indY].plot(fore, color='black', label='Forecast')
handles, labels = axs[2, 2].get legend handles labels()
fig.legend(handles, labels, loc='upper right')
print(sse)
fig, axs = plt.subplots(3, 3, figsize=(15, 12))
plt.rcParams.update({'font.size': 15, 'xtick.labelsize': 10,
'vtick.labelsize': 10})
indX = 0
indY = 0
sse = []
for countr in countries:
 dfCountry = df[df['Country name'] == countr]
 X = dfCountry.set index('year')['Life Ladder']
 meanX = X.mean()
 X = X.reindex(range(2015, 2021), fill_value=meanX)
 X.index = pd.to datetime(X.index, format='%Y')
 fit = Holt(X).fit()
 sse.append(fit.sse)
 Yhat = fit.fittedvalues
 fore = fit.forecast(2)
 fore.index = fore.index.year
 print(countr)
 print(fore)
 print(fit.sse)
  axs[indX, indY].plot(X.index.year, X, color='blue', label='Actual')
```

```
axs[indX, indY].set title(countr)
  axs[indX, indY].set ylim(0, 9)
  axs[indX, indY].set xlim(2015, 2022)
  axs[indX, indY].plot(Yhat.index.year, Yhat, color='red', label='Fitted
values')
  axs[indX, indY].plot(fore, color='black', label='Forecast')
  indX += 1
  if indX > 2:
    indX = 0
    indY += 1
X = df.groupby('year')['Life Ladder'].mean()
meanX = X.mean()
X = X.reindex(range(2015, 2021), fill value=meanX)
X.index = pd.to datetime(X.index, format='%Y')
axs[2, 2].plot(X.index.year, X, color='blue', label='Actual')
axs[2, 2].set title('Average overall')
axs[2, 2].set ylim(0, 9)
axs[2, 2].set xlim(2015, 2022)
fit = Holt(X).fit()
sse.append(fit.sse)
Yhat = fit.fittedvalues
fore = fit.forecast(2)
fore.index = fore.index.year
print('World average')
print(fore)
print(fit.sse)
axs[2, 2].plot(Yhat.index.year, Yhat, color='red', label='Fitted values')
axs[indX, indY].plot(fore, color='black', label='Forecast')
handles, labels = axs[2, 2].get legend handles labels()
fig.legend(handles, labels, loc='upper right')
print(sse)
```

References

- Folaraz. (2017, October) . World Countries and Continents Details, Version 3. Retrieved April 27, 2021 from https://www.kaggle.com/folaraz/world-countries-and-continents-details
- Helliwell, John F., Richard Layard, Jeffrey Sachs, and Jan-Emmanuel De Neve. (2021). World Happiness Report 2021. New York: Sustainable Development Solutions Network.

Retrieved April 27, 2021 from

https://worldhappiness.report/ed/2021/#appendices-and-data

Raschka, Sebastian. "Sequential Feature Selector." Mlxtend, MkDocs,

rasbt.github.io/mlxtend/user_guide/feature_selection/SequentialFeatureSelector/

World Bank, World Development Indicators. (2017) . *Indicators*. Retrieved April 27, 2021 from https://data.worldbank.org/indicator